

Future Extension to Multi-objective Performance-based Sustainable Design



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SELIM GÜNAY, POST-DOC

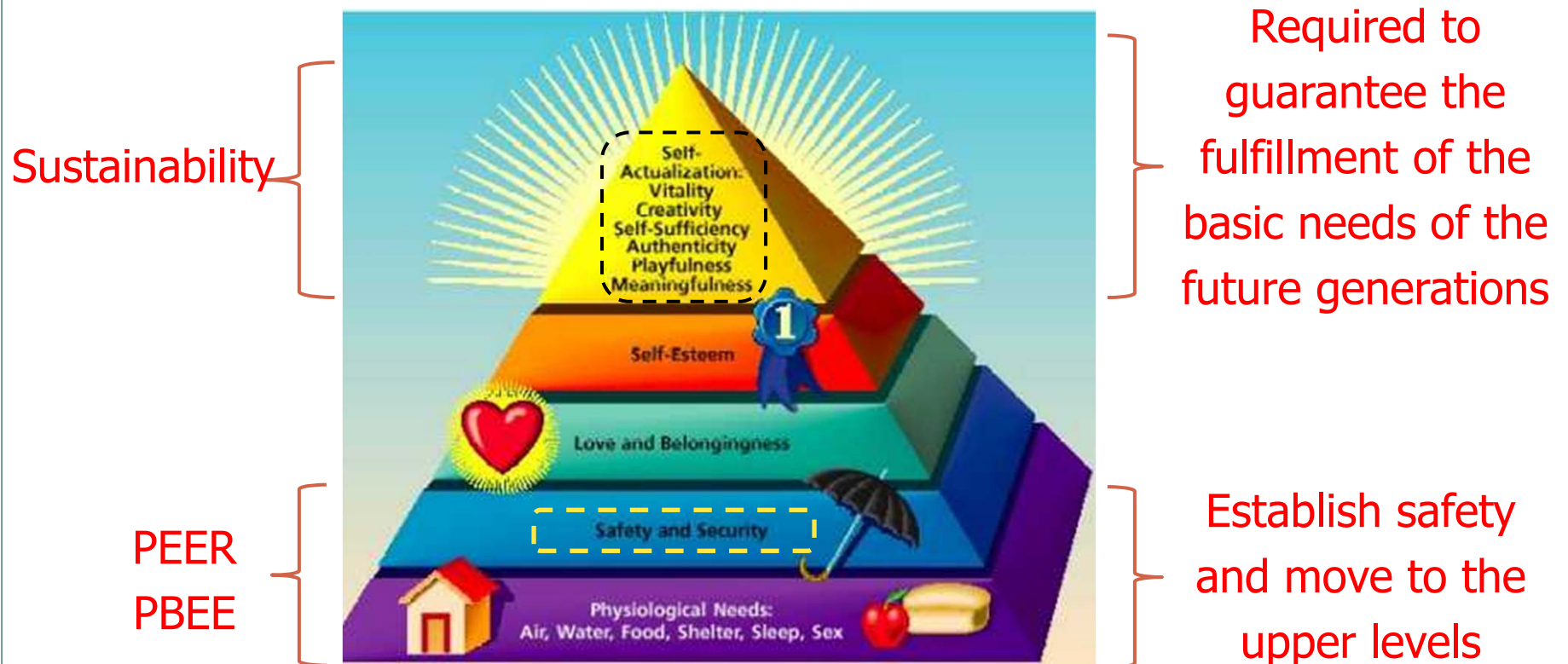
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Introduction



Analogy to Hierarchy of Needs (Maslow, 1963)



Introduction



Analogy to Hierarchy of Needs (Maslow, 1963)

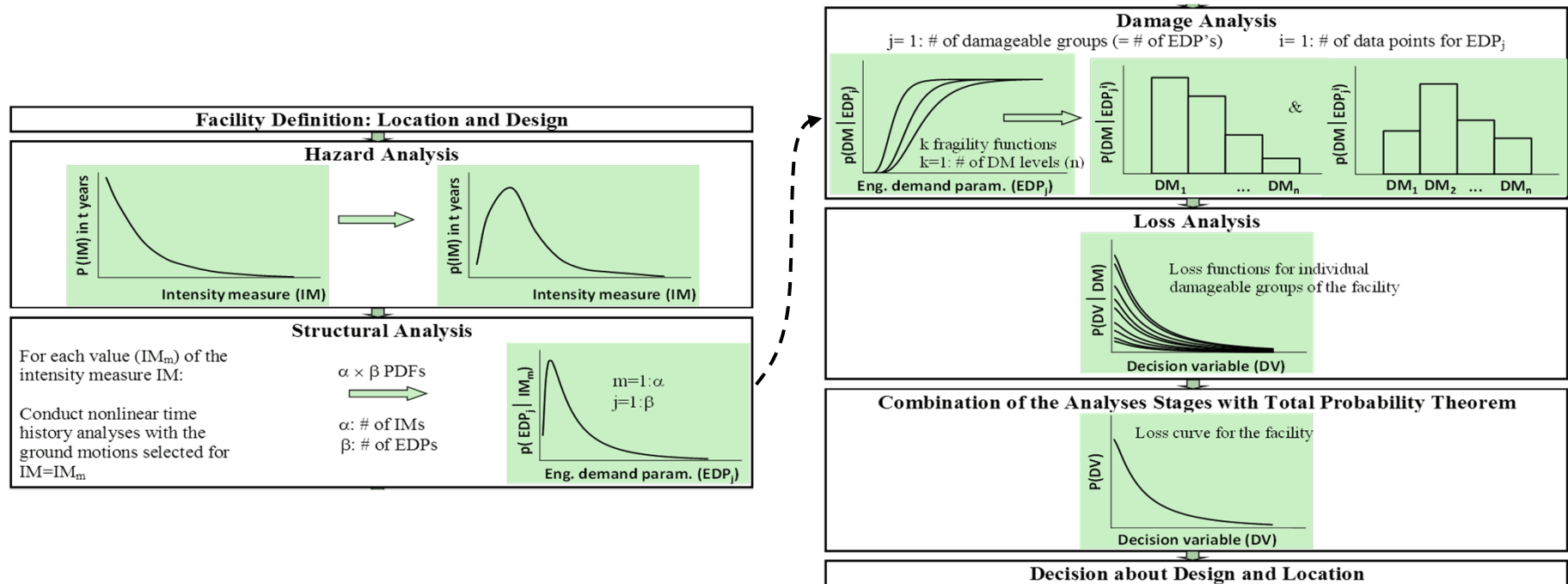
- ❑ **Basic Needs: Safety Objective** → PEER PBEE Probabilistic Formulation
- ❑ **Upper Level Needs** for sustainability: Environmental safety and human comfort objectives → **Uncertain and probabilistic by nature**
- ❑ Motivation for an inherent **extension of PEER methodology to a generalized probabilistic multi-objective framework**

| Objective | Required Analysis Type | | | | | | |
|------------------------------|------------------------|------------|--------|---------|--------|----------------|-----------------|
| | Hazard | Structural | Damage | Climate | Energy | Sustainability | Life Cycle Cost |
| Structural Safety | ✓ | ✓ | ✓ | | | | ✓ |
| Environmental Responsibility | | | | ✓ | ✓ | ✓ | ✓ |
| Human Comfort | | | | ✓ | ✓ | ✓ | ✓ |

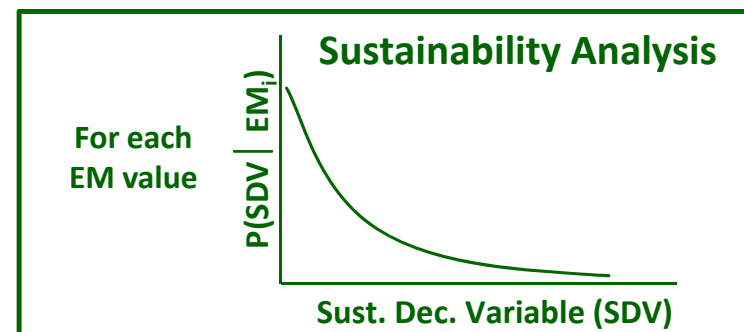
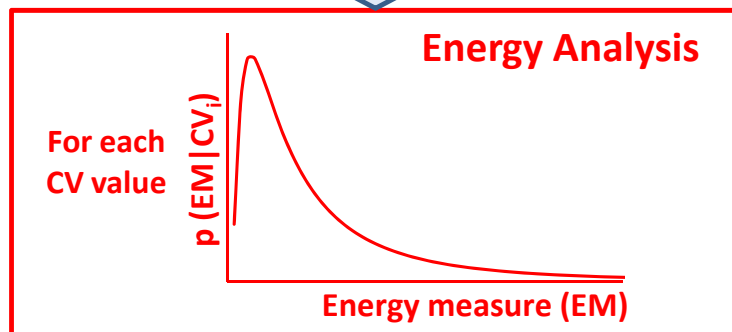
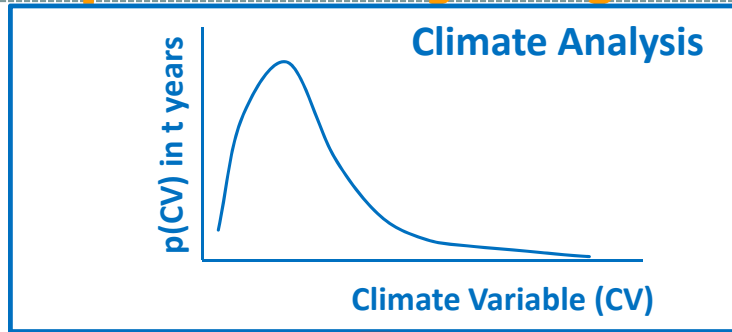
Extended Framework: Safety Objective

Structural Safety Objective:

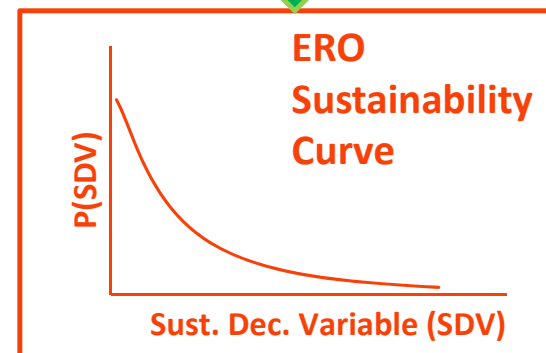
$$P(DV) = \int \int \int P(DV|DM) p(DM|EDP) p(EDP|IM) p(IM) dIM dEDP dDM$$



Extended Framework: Environmental Responsibility Objective (ERO): Sustainability



$$P(SDV) = \iint P(SDV | EM) p(EM | CV) p(CV) dCV dEM$$

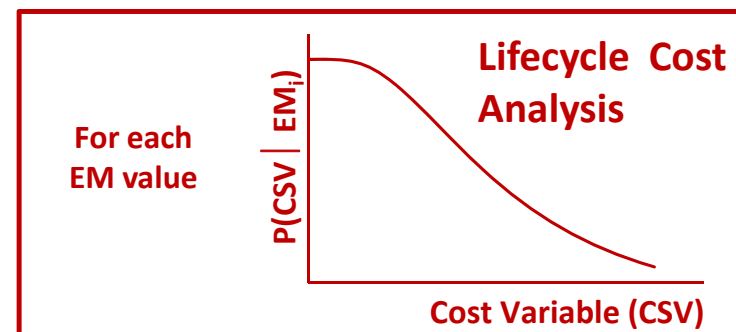
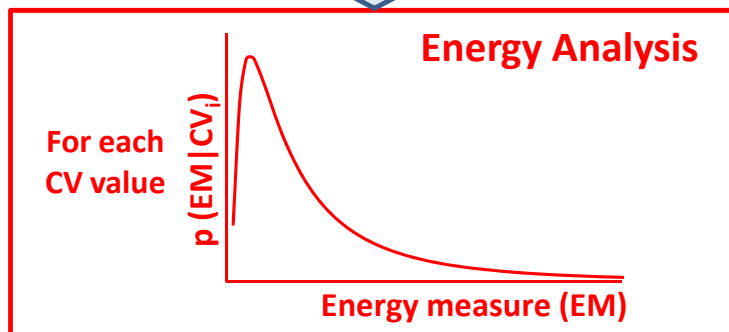
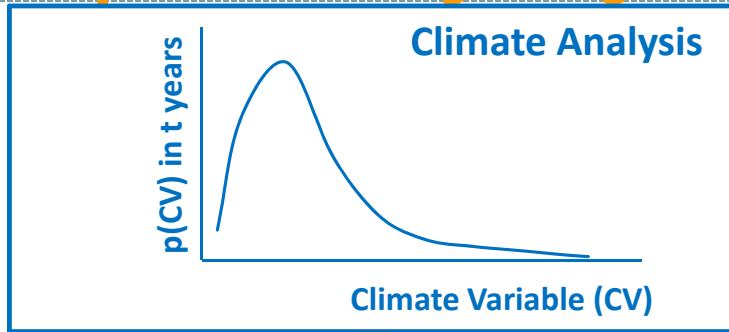


Extended Framework: Environmental Responsibility Objective (ERO): Sustainability

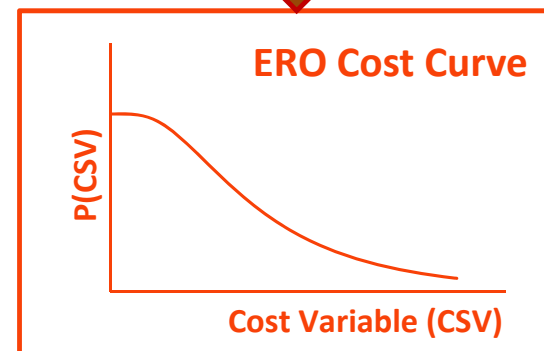
$$P(\text{SDV}) = \iint \underbrace{P(\text{SDV} | \text{EM})}_{\text{Sustainability Analysis}} \underbrace{p(\text{EM} | \text{CV})}_{\text{Energy Analysis}} \underbrace{p(\text{CV})}_{\text{Climate Analysis}} d\text{CV} d\text{EM}$$

- SDV** : Sustainability Decision Variable, e.g. Carbon or ecological footprint
EM : Energy measure, e.g. Building energy
CV : Climate Variable, e.g. Temperature change

Extended Framework: Environmental Responsibility Objective (ERO): Life Cycle Cost



$$P(CSV) = \iint P(CSV | EM) p(EM | CV) p(CV) dCV dEM$$



Extended Framework: Environmental Responsibility Objective (ERO): Life Cycle Cost

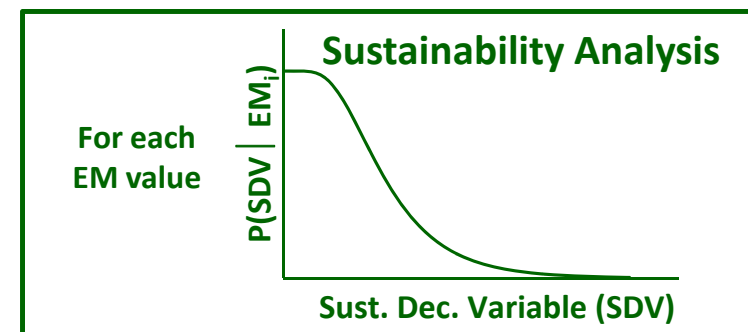
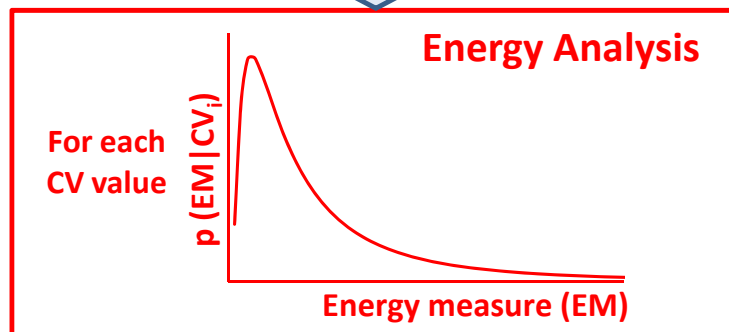
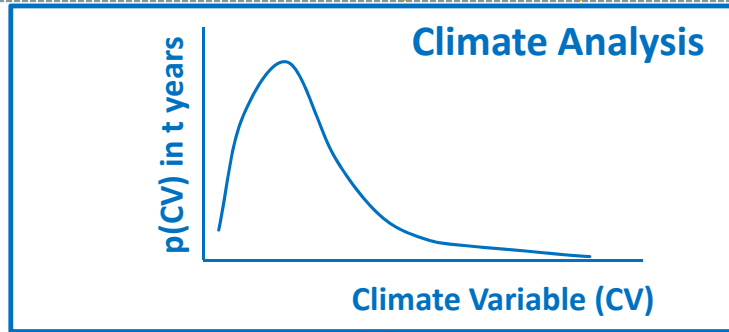
$$P(\text{CSV}) = \iint \underbrace{P(\text{CSV} | \text{EM})}_{\text{Lifecycle Cost Analysis}} \underbrace{p(\text{EM} | \text{CV})}_{\text{Energy Analysis}} \underbrace{p(\text{CV})}_{\text{Climate Analysis}} d\text{CV} d\text{EM}$$

CSV: Cost/Saving Variable, e.g. Ratio initial cost/savings during lifecycle

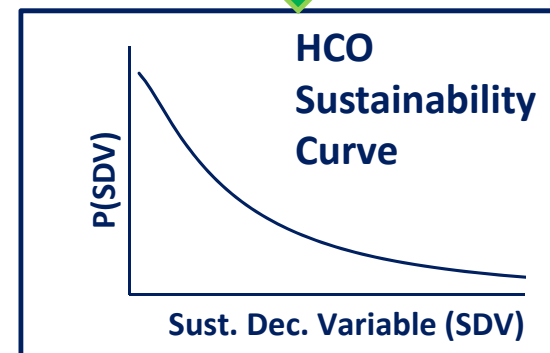
EM: Energy measure, e.g. Energy consumption

CV: Climate Variable, e.g. Temperature change

Extended Framework: Human Comfort Objective (HCO): Sustainability



$$P(SDV) = \iint P(SDV | EM) p(EM | CV) p(CV) dCV dEM$$



Extended Framework: Human Comfort Objective (HCO): Sustainability

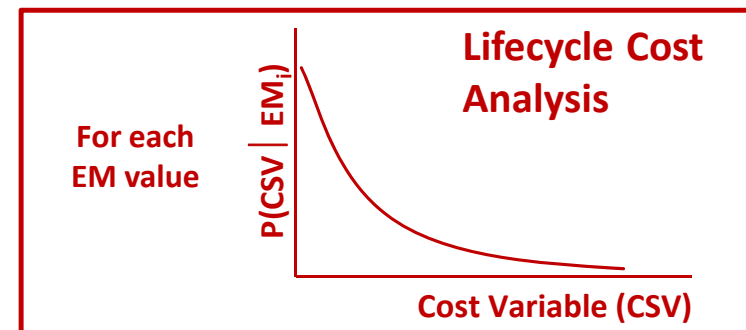
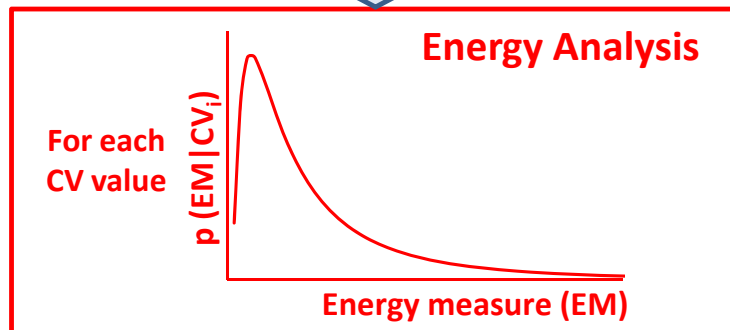
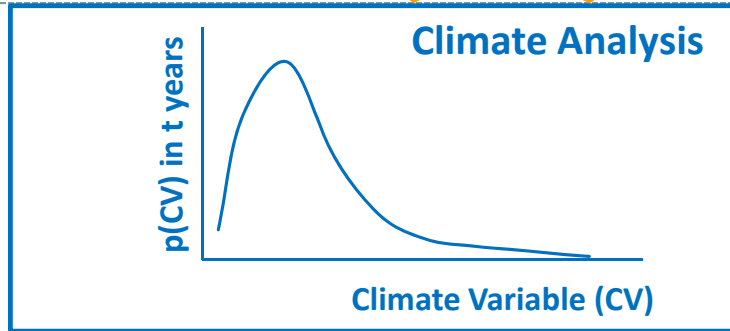
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SDV : Sustainability Decision Variable, e.g. Human productivity

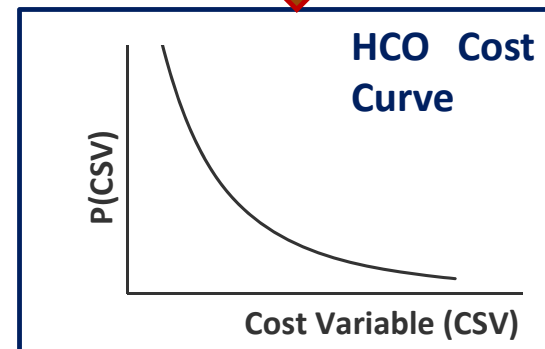
EM : Energy measure, e.g. Energy consumption

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Extended Framework: Human Comfort Objective (HCO): Life Cycle Cost



$$P(CSV) = \iint P(CSV | EM) p(EM | CV) p(CV) dCV dEM$$



Extended Framework: Human Comfort Objective (HCO): Life Cycle Cost

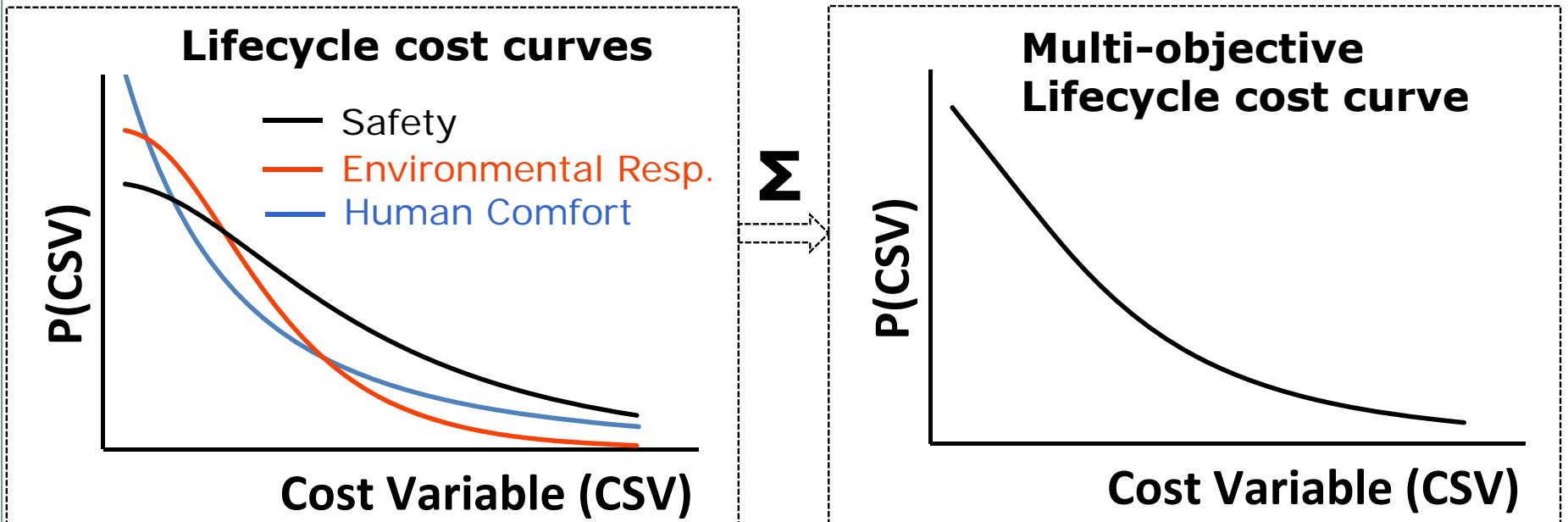
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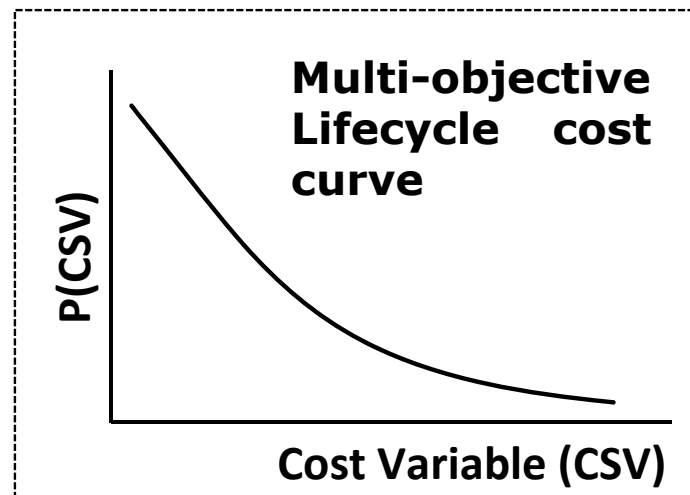
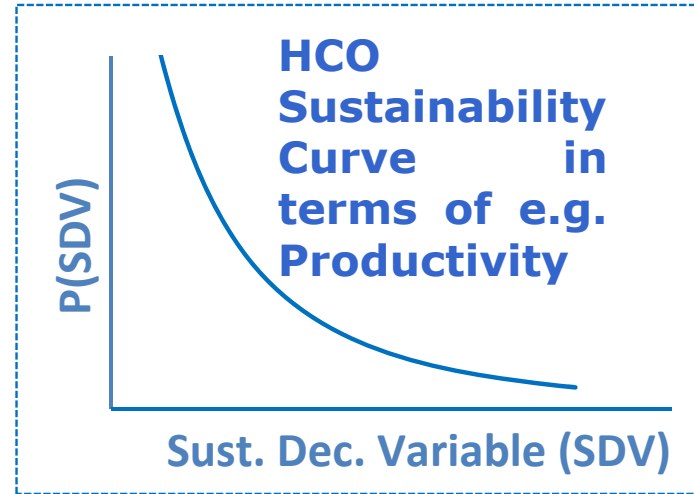
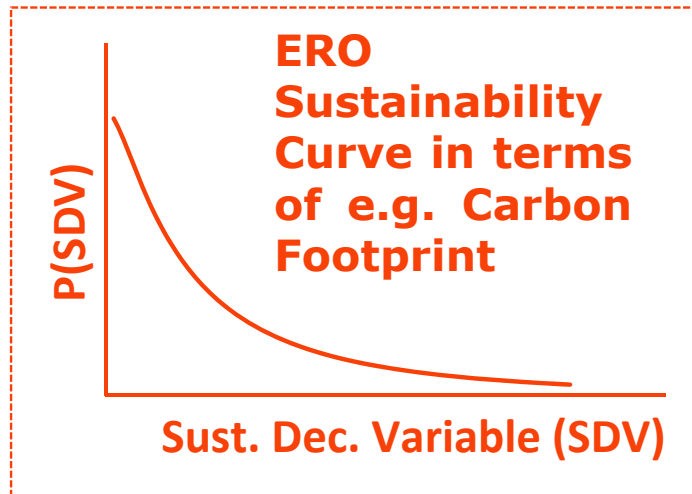
EM : Energy measure, e.g. Energy consumption

CV : Climate Variable, e.g. Temperature change

Extended Framework: Multi-objective Life Cycle Cost



Extended Framework: **Decision Tools**



Extended Framework: **Systematic Decision**



Obtained products (**previous slide**) can be used in a systematic manner for decision making

❑ **Decision-Making Systems**

- Is preference information required?
- Is preference information presented as relative weights?
- Will the weights be generated during the process?

❑ **MIVES (Model for Integration of Values for Evaluation of Sustainability): Decision-Making Process**

- Tree Construction
- Value Function
- Weight Assignment
- Overall Evaluation and Selection of the Best Solution

Extended Framework: **Systematic Decision**



❑ **MIVES: Decision-Making Process**

▪ **Tree Construction**

San José and Garrucho (2010); Pons (2011)

- ✓ Objectives
- ✓ Relevance
- ✓ Difference-making for each one of the alternatives
- ✓ Minimal number of items

Iyengar (2012)

- ✓ Cut: Use 3 levels of unfolded branches, and every branch to have 5 sub-branches or less in the successive unfolding steps;
- ✓ Concretize: Use indicators that experts and stakeholders can understand;
- ✓ Categorize: Use more categories and fewer choices; and
- ✓ Gradually increase the complexity.

Extended Framework: Systematic Decision

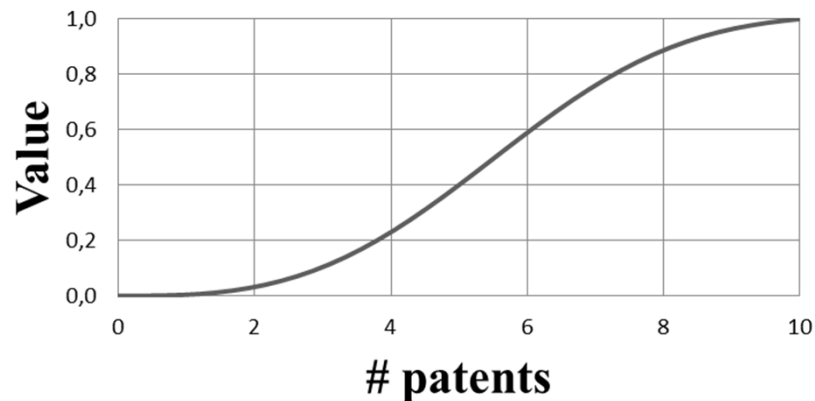


□ MIVES: Decision-making Process

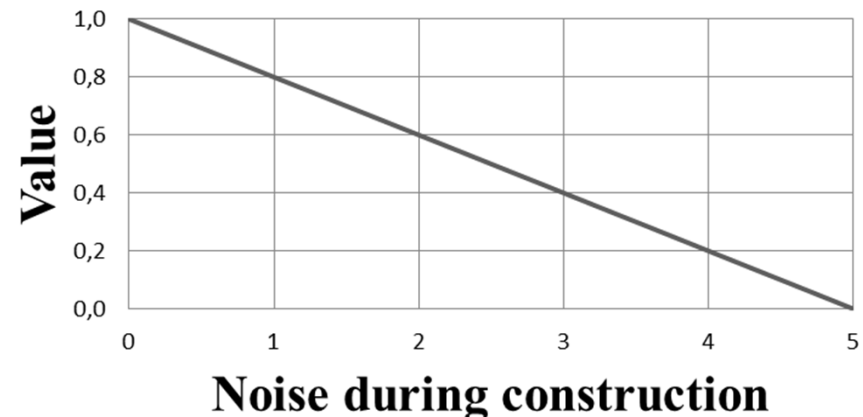
▪ Value Functions

- ✓ Non-negative increasing/decreasing functions, $0 \leq V^i(X_k^i) \leq 1$
- ✓ Linear, concave, convex, S-shaped, etc.
- ✓ Presence of value functions allows for consideration of a broad range of indicators and eliminates need for using indicators with same units.

Examples



Number of new patents used in building design



Annoyance to neighbours (noise) during construction

Extended Framework: Systematic Decision

□ MIVES: Decision-making Process

▪ Weight Assignment

| Requirement | W_{req} % | Criteria | W_{crit} % | i | Indicator | W_{ind} % | Unit |
|---------------|-------------|-------------------------|--------------|----------|--------------------------|-------------|----------------|
| Functional | 10.0 | Quality perception | 30.0 | 1 | User | 75.0 | 0-5 |
| | | | | 2 | Visitor | 25.0 | 0-5 |
| | | Adaptability to changes | 70.0 | 3 | Modularity | 100.0 | % |
| Economic | 50.0 | Construction cost | 50.0 | 4 | Direct cost | 80.0 | \$ |
| | | | | 5 | Deviation | 20.0 | % |
| | | Life cost | 50.0 | 6 | Utilization | 40.0 | \$ |
| | | | | 7 | Maintenance | 30.0 | \$ |
| | | | | 8 | Losses | 30.0 | \$ |
| Social | 20.0 | Integration of science | 10.0 | 9 | New patents | 100.0 | # |
| | | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ |
| Environmental | 20.0 | Construction | 20.0 | 15 | Water consumption | 10.0 | m ³ |
| | | | | 16 | CO ₂ emission | 40.0 | Kg |
| | | | | 17 | Energy consumption | 10.0 | MJ |
| | | | | 18 | Raw materials | 20.0 | Kg |
| | | | | 19 | Solid waste | 20.0 | Kg |
| | | Utilization | 40.0 | 20 | Noise, dust, smell | 10.0 | 0-5 |
| | | | | 21 | Energy consumption | 45.0 | MJ/year |
| | | | | 22 | CO ₂ emission | 45.0 | kg/year |
| | | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ |

See slide 4

Extended Framework: Systematic Decision



□ MIVES: Decision-making Process

▪ Selection Amongst Alternatives

Integration of values of every indicator of any alternative k

$$V_k = \sum_{i=1}^{N_{ind}} W_{req}^i \cdot W_{crit}^i \cdot W_{ind}^i \cdot V^i(X_k^i)$$

Weights Value function

- ✓ The value of each alternative is determined → The alternative that has the highest value, i.e. closest to 1.0, becomes the most suitable alternative, i.e. the “best” solution.

Extended Framework: Systematic Decision



□ PBE approach: PBE-MIVES

▪ Multiple Indicators in a Direct Probabilistic Manner

Assume **3** indicators DV_{CO_2} , DV_E and DV_{ST} are considered and corresponding PDFs are:

$$f_{CO_2}(DV_{CO_2} = a) = A, \quad f_E(DV_E = b) = B, \quad f_{ST}(DV_{ST} = c) = C$$

For weights w_{CO_2} , w_E and w_{ST} , the overall value for the indicators is:

$$V(a, b, c) = V_{CO_2}(a) + V_E(b) + V_{ST}(c) = w_{CO_2}u_{CO_2}(a) + w_Eu_E(b) + w_{ST}u_{ST}(c)$$

If DV_{CO_2} , DV_E and DV_{ST} (with value functions u_{CO_2} , u_E , and u_{ST}) are **mutually independent**, the joint PDF is:

$$\begin{aligned} f(a, b, c) &= f_{CO_2, E, ST}(DV_{CO_2} = a, DV_E = b, DV_{ST} = c) \\ &= f_{CO_2}(DV_{CO_2} = a) f_E(DV_E = b) f_{ST}(DV_{ST} = c) = ABC \end{aligned}$$

else,

$$\begin{aligned} f(a, b, c) &= f_{CO_2, E, ST}(DV_{CO_2} = a, DV_E = b, DV_{ST} = c) \\ &= f_{CO_2}(DV_{CO_2} = a) f_{E|CO_2}(DV_E = b | DV_{CO_2} = a) f_{ST|CO_2, E}(DV_{ST} = c | DV_{CO_2} = a, DV_E = b) \end{aligned}$$

Therefore, **the conditional probability distribution** should be defined.

$$P(DV^n = a) = p(DV > DV^n = a) = \int_a^\infty f_{DV}(DV) d(DV)$$

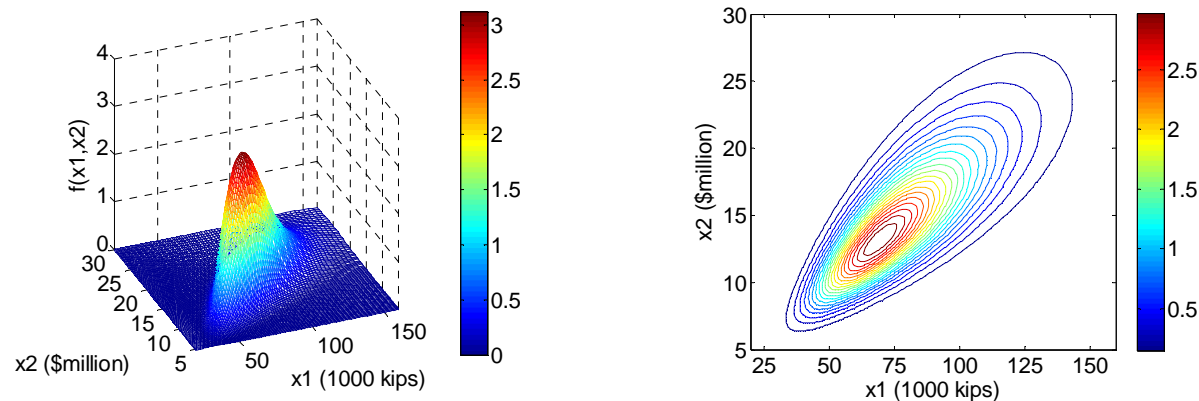
where $P(DV^n)$ is the POE of n^{th} value of DV , and $p(DV > DV^n = a)$ is the probability of DV exceeding a , n^{th} value of DV .

Extended Framework: Systematic Decision

□ PBE approach: PBE-MIVES

▪ Application to the UCS Building

- ✓ Two alternatives with different fuel consumption (in Btu) ratios
Electricity : Natural gas = 5 : 2 (**Plan 1**), Electricity only (**Plan 2**)
- ✓ Bivariate lognormal distribution assumed for energy expenditure and CO₂ emission for **50** years (**building life span**).
- ✓ Each mean value estimated based on data for **office buildings** in the West-Pacific region (by DOE, EIA, & EPA).
- ✓ Standard deviation assumed as 30% of the corresponding mean value.
- ✓ Coefficient of correlation was assumed as 0.8.



Probability density function of energy expenditure (x_1) and CO₂ emission (x_2) for **Plan 1**

Extended Framework: Systematic Decision

□ PBE approach: PBE-MIVES

▪ Application to the UCS Building

| Requirement | W_r [%] | Criteria | i | Indicator | W_i [%] | Unit |
|---------------|-----------|-------------|-----|---------------------------|-----------|-----------|
| Environmental | 25.0 | Utilization | 1 | CO ₂ emissions | 100.0 | 1000 kips |
| Economic | 75.0 | Life cost | 2 | Energy expenditures | 60.0 | \$million |
| | | | 3 | Losses | 40.0 | \$million |

Linearly decreasing value functions

$$\begin{aligned}
 u(x) &= 1.0 \quad \text{if } x \leq x_a \\
 &= 1.0 - (x - x_a)/(x_b - x_a) \quad \text{if } x_a < x \leq x_b \\
 &= 0.0 \quad \text{if } x > x_b
 \end{aligned}$$

→ The following was computed to compare Plans 1 and 2:

$$V_{prob} = \int_{\Omega} V f d\Omega$$

Expected value of an alternative → rank different alternatives

If no loss, i.e. $x_3 = 0$

Case 1: $0 \leq x_1 \leq 80, 0 \leq x_2 \leq 15$

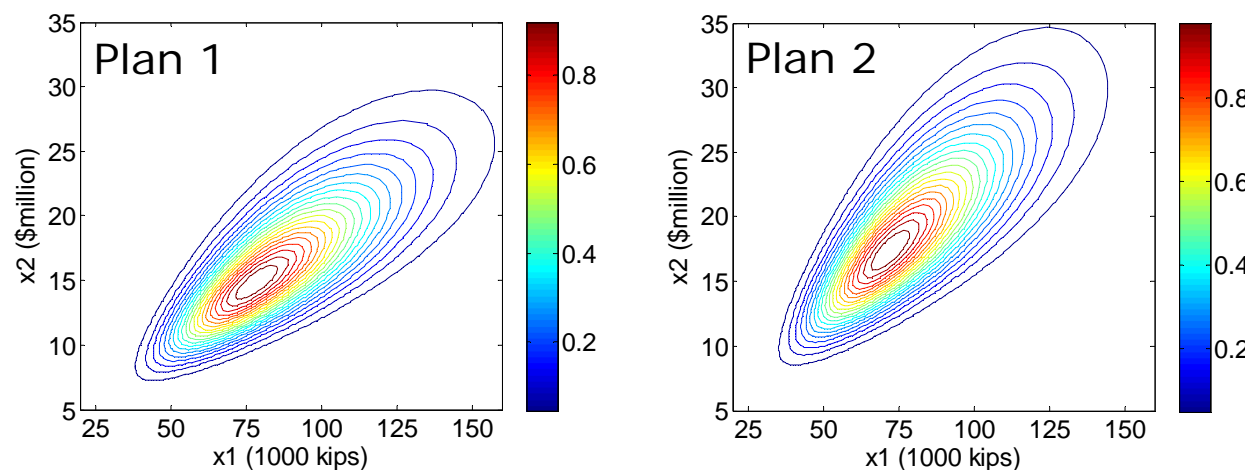
✓ Plan 1: $V_{prob} = 309.52$

Plan 2: $V_{prob} = 223.56$

Case 2: $0 \leq x_1 \leq 80, 0 \leq x_2 \leq 20$

Plan 1: $V_{prob} = 393.95$

✓ Plan 2: $V_{prob} = 449.61$



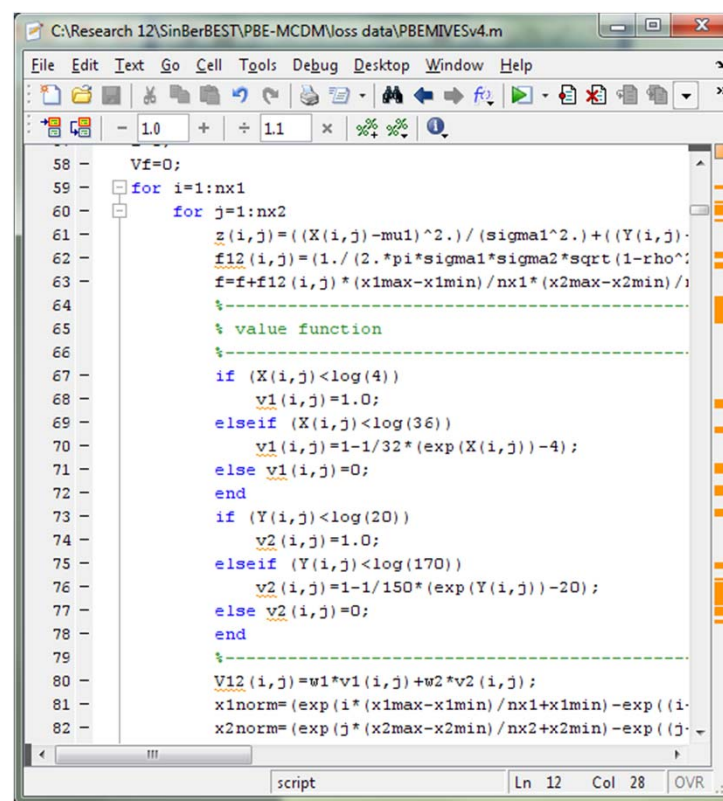
Contours of Vf of energy expenditures (x_1) and CO₂ emissions (x_2) for Plans 1 and 2 of the UCS example building
 [Monetary loss due to structural damages $x_3 = 0$]

Extended Framework: Systematic Decision

□ PBE approach: PBE-MIVES

- ✓ The probabilistic nature of the indicators can be considered in MCDA either indirectly by the calculation of the value of each indicator in a probabilistic manner or directly by formulating the value determination equation in a probabilistic framework.
- ✓ The correlation between the different indicators is taken into account in the direct formulation and it is the preferred method when there is significant interdependency between indicators.
- ✓ As shown in the comparison of V_{prob} in the UCS example building, considered range of indicators can change the value of the alternatives and affect the final decision. Therefore, attention should be paid to the selection of the proper range of indicators.

Matlab code for PBE-MIVES



```
58 - Vf=0;
59 - for i=1:nx1
60 -     for j=1:nx2
61 -         z(i,j)=((X(i,j)-mu1)^2.)/(sigma1^2.)+(Y(i,j)-
62 -         f12(i,j)=(1./(2.*pi*sigma1*sigma2*sqrt(1-rho^
63 -         f=f+f12(i,j)*(x1max-x1min)/nx1*(x2max-x2min)/)
64 -         % value function
65 -         % -----
66 -         if (X(i,j)<log(4))
67 -             v1(i,j)=1.0;
68 -         elseif (X(i,j)<log(36))
69 -             v1(i,j)=1-1/32*(exp(X(i,j))-4);
70 -         else v1(i,j)=0;
71 -         end
72 -         if (Y(i,j)<log(20))
73 -             v2(i,j)=1.0;
74 -         elseif (Y(i,j)<log(170))
75 -             v2(i,j)=1-1/150*(exp(Y(i,j))-20);
76 -         else v2(i,j)=0;
77 -         end
78 -         % -----
79 -         V12(i,j)=w1*v1(i,j)+w2*v2(i,j);
80 -         x1norm=(exp(i*(x1max-x1min)/nx1+x1min)-exp((i-
81 -         x2norm=(exp(j*(x2max-x2min)/nx2+x2min)-exp((j-
```



Thank you